

Package ‘bbotk’

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Title Black-Box Optimization Toolkit

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Description Provides a common framework for optimization of black-box functions for other packages, e.g. 'mlr3tuning' or 'mlr3fselect'. It offers various optimization methods e.g. grid search, random search and generalized simulated annealing.

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URL <https://bbotk.mlr-org.com>, <https://github.com/mlr-org/bbotk>

BugReports <https://github.com/mlr-org/bbotk/issues>

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'TerminatorPerfReached.R' 'TerminatorRunTime.R'
 'TerminatorStagnation.R' 'TerminatorStagnationBatch.R'
 'assertions.R' 'bbotk_reflections.R' 'bibentries.R' 'helper.R'
 'sugar.R' 'zzz.R'

Author Marc Becker [cre, aut] (<<https://orcid.org/0000-0002-8115-0400>>),
 Jakob Richter [aut] (<<https://orcid.org/0000-0003-4481-5554>>),
 Michel Lang [aut] (<<https://orcid.org/0000-0001-9754-0393>>),
 Bernd Bischl [aut] (<<https://orcid.org/0000-0001-6002-6980>>),
 Martin Binder [aut],
 Olaf Mersmann [ctb]

Maintainer Marc Becker <marcbecker@posteo.de>

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bbotk-package

bbotk: Black-Box Optimization Toolkit

Description

Provides a common framework for optimization of black-box functions for other packages, e.g. 'mlr3tuning' or 'mlr3fselect'. It offers various optimization methods e.g. grid search, random search and generalized simulated annealing.

Author(s)

Maintainer: Marc Becker <marcbecker@posteo.de> ([ORCID](#))

Authors:

- Jakob Richter <jakob1richter@gmail.com> ([ORCID](#))
- Michel Lang <michellang@gmail.com> ([ORCID](#))
- Bernd Bischl <bernd_bischl@gmx.net> ([ORCID](#))
- Martin Binder <martin.binder@mail.com>

Other contributors:

- Olaf Mersmann <olafm@statistik.tu-dortmund.de> [contributor]

See Also

Useful links:

- <https://bbotk.mlr-org.com>
- <https://github.com/mlr-org/bbotk>
- Report bugs at <https://github.com/mlr-org/bbotk/issues>

Archive

Logging object for objective function evaluations

Description

Container around a `data.table::data.table` which stores all performed function calls of the Objective.

Public fields

- `search_space` ([paradox::ParamSet](#))
Search space of objective.
- `codomain` ([paradox::ParamSet](#))
Codomain of objective function.
- `start_time` ([POSIXct](#))
Time stamp of when the optimization started. The time is set by the [Optimizer](#).
- `check_values` (`logical(1)`)
Determines if points and results are checked for validity.
- `data` ([data.table::data.table](#))
Contains all performed [Objective](#) function calls.
- `store_x_domain` (`logical(1)`)
Determines if x values, should be stored in `$data$x_domain` as list items. The trafo will be applied if defined in `search_space`.

Active bindings

- `n_evals` (`integer(1)`)
Number of evaluations stored in the archive.
- `n_batch` (`integer(1)`)
Number of batches stored in the archive.
- `cols_x` (`character()`)
Column names of search space parameters.
- `cols_y` (`character()`)
Column names of codomain parameters.

Methods**Public methods:**

- [Archive\\$new\(\)](#)
- [Archive\\$add_evals\(\)](#)
- [Archive\\$best\(\)](#)
- [Archive\\$format\(\)](#)
- [Archive\\$print\(\)](#)
- [Archive\\$clear\(\)](#)
- [Archive\\$clone\(\)](#)

Method `new()`: Creates a new instance of this [R6](#) class.

Usage:

```
Archive$new(search_space, codomain, check_values = TRUE, store_x_domain = TRUE)
```

Arguments:

`search_space` ([paradox::ParamSet](#))

Specifies the search space for the [Optimizer](#). The [paradox::ParamSet](#) describes either a subset of the domain of the [Objective](#) or it describes a set of parameters together with a trafo function that transforms values from the search space to values of the domain. Depending on the context, this value defaults to the domain of the objective.

`codomain` ([paradox::ParamSet](#))

Specifies codomain of function. Most importantly the tags of each output "Parameter" define whether it should be minimized or maximized. The default is to minimize each component.

`check_values` (`logical(1)`)

Should x-values that are added to the archive be checked for validity? Search space that is logged into archive.

`store_x_domain` (`logical(1)`)

Determines if x values, should be stored in `$data$x_domain` as list items. The trafo will be applied if defined in `search_space`.

Method `add_evals()`: Adds function evaluations to the archive table.

Usage:

```
Archive$add_evals(xdt, xss_trafoed = NULL, ydt)
```

Arguments:

`xdt` ([data.table::data.table\(\)](#))

Set of untransformed points / points from the *search space*. One point per row, e.g. `data.table(x1 = c(1, 3), x2 = c(2, 4))`. Column names have to match ids of the `search_space`. However, `xdt` can contain additional columns.

`xss_trafoed` (`list()`)

Transformed point(s) in the *domain space*. Not stored and needed if `store_x_domain = FALSE`.

`ydt` ([data.table::data.table\(\)](#))

Optimal outcome.

Method `best()`: Returns the best scoring evaluation. For single-crit optimization, the solution that minimizes / maximizes the objective function. For multi-crit optimization, the Pareto set / front.

Usage:

```
Archive$best(batch = NULL)
```

Arguments:

`batch` (`integer()`)

The batch number(s) to limit the best results to. Default is all batches.

Returns: [data.table::data.table\(\)](#).

Method `format()`: Helper for print outputs.

Usage:

```
Archive$format()
```

Method `print()`: Printer.

Usage:

Archive\$print()

Arguments:

... (ignored).

Method clear(): Clear all evaluation results from archive.

Usage:

Archive\$clear()

Method clone(): The objects of this class are cloneable with this method.

Usage:

Archive\$clone(deep = FALSE)

Arguments:

deep Whether to make a deep clone.

ArchiveBest

Minimal logging object for objective function evaluations

Description

The [ArchiveBest](#) stores no data but records the best scoring evaluation passed to `$add_evals()`. The [Archive](#) API is fully implemented but many parameters are ignored and some methods do nothing. The archive still works with [TerminatorClockTime](#), [TerminatorEvals](#), [TerminatorNone](#) and [TerminatorEvals](#).

Super class

`bbotk::Archive` -> ArchiveBest

Active bindings

n_evals (integer(1))

Number of evaluations stored in the archive.

n_batch (integer(1))

Number of batches stored in the archive.

Methods

Public methods:

- [ArchiveBest\\$new\(\)](#)
- [ArchiveBest\\$add_evals\(\)](#)
- [ArchiveBest\\$best\(\)](#)
- [ArchiveBest\\$clone\(\)](#)

Method new(): Creates a new instance of this [R6](#) class.

Usage:

```
ArchiveBest$new(
  search_space,
  codomain,
  check_values = FALSE,
  store_x_domain = FALSE
)
```

Arguments:

search_space ([paradox::ParamSet](#))

Specifies the search space for the [Optimizer](#). The [paradox::ParamSet](#) describes either a subset of the domain of the [Objective](#) or it describes a set of parameters together with a trafo function that transforms values from the search space to values of the domain. Depending on the context, this value defaults to the domain of the objective.

codomain ([paradox::ParamSet](#))

Specifies codomain of function. Most importantly the tags of each output "Parameter" define whether it should be minimized or maximized. The default is to minimize each component.

check_values (logical(1))

ignored.

store_x_domain (logical(1))

Determines if x values, should be stored in `$data$x_domain` as list items. The trafo will be applied if defined in search_space.

Method `add_evals()`: Stores the best result in ydt.

Usage:

```
ArchiveBest$add_evals(xdt, xss_trafoed = NULL, ydt)
```

Arguments:

xdt ([data.table::data.table\(\)](#))

Set of untransformed points / points from the *search space*. One point per row, e.g. `data.table(x1 = c(1, 3), x2 = c(2, 4))`. Column names have to match ids of the search_space. However, xdt can contain additional columns.

xss_trafoed (`list()`)

Transformed point(s) in the *domain space*.

ydt ([data.table::data.table\(\)](#))

Optimal outcome.

Method `best()`: Returns the best scoring evaluation. For single-crit optimization, the solution that minimizes / maximizes the objective function. For multi-crit optimization, the Pareto set / front.

Usage:

```
ArchiveBest$best(m = NULL)
```

Arguments:

m (`integer()`)

ignored.

Returns: [data.table::data.table\(\)](#)

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
ArchiveBest$clone(deep = FALSE)
```

Arguments:

`deep` Whether to make a deep clone.

<code>is_dominated</code>	<i>Calculate which points are dominated</i>
---------------------------	---

Description

Calculates which points are not dominated, i.e. points that belong to the Pareto front.

Usage

```
is_dominated(yamat)
```

Arguments

<code>yamat</code>	(<code>matrix()</code>) A numeric matrix. Each column (!) contains one point.
--------------------	--

<code>mlr_optimizers</code>	<i>Dictionary of Optimizer</i>
-----------------------------	--------------------------------

Description

A simple `mlr3misc::Dictionary` storing objects of class `Optimizer`. Each optimizer has an associated help page, see `mlr_optimizer_[id]`.

This dictionary can get populated with additional optimizer by add-on packages.

For a more convenient way to retrieve and construct optimizer, see `opt()/opts()`.

Format

`R6::R6Class` object inheriting from `mlr3misc::Dictionary`.

Methods

See `mlr3misc::Dictionary`.

See Also

Sugar functions: `opt()`, `opts()`

Examples

```
opt("random_search", batch_size = 10)
```


Description

OptimizerCmaes class that implements CMA-ES. Calls `adagio::pureCMAES()` from package **adagio**.

Dictionary

This `Optimizer` can be instantiated via the dictionary `mlr_optimizers` or with the associated sugar function `opt()`:

```
mlr_optimizers$get("cmaes")
opt("cmaes")
```

Parameters

`sigma` numeric(1)

`start_values` character(1)

Create random start values or based on center of search space? In the latter case, it is the center of the parameters before a trafo is applied.

For the meaning of the control parameters, see `adagio::pureCMAES()`. Note that we have removed all control parameters which refer to the termination of the algorithm and where our terminators allow to obtain the same behavior.

Progress Bars

`$optimize()` supports progress bars via the package **progressr** combined with a `Terminator`. Simply wrap the function in `progressr::with_progress()` to enable them. We recommend to use package **progress** as backend; enable with `progressr::handlers("progress")`.

Super class

```
bbotk::Optimizer -> OptimizerCmaes
```

Methods

Public methods:

- `OptimizerCmaes$new()`
- `OptimizerCmaes$clone()`

Method `new()`: Creates a new instance of this R6 class.

Usage:

```
OptimizerCmaes$new()
```

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
OptimizerCmaes$clone(deep = FALSE)
```

Arguments:

deep Whether to make a deep clone.

Examples

```
if(requireNamespace("adagio")) {
  library(paradox)

  domain = ParamSet$new(list(ParamDbf$new("x", lower = -1, upper = 1)))

  search_space = ParamSet$new(list(ParamDbf$new("x", lower = -1, upper = 1)))

  codomain = ParamSet$new(list(ParamDbf$new("y", tags = "minimize")))

  objective_function = function(xs) {
    list(y = as.numeric(xs)^2)
  }

  objective = ObjectiveRfun$new(fun = objective_function,
                                domain = domain,
                                codomain = codomain)

  terminator = trm("evals", n_evals = 10)
  instance = OptimInstanceSingleCrit$new(
    objective = objective,
    search_space = search_space,
    terminator = terminator)

  optimizer = opt("cmaes")

  # Modifies the instance by reference
  optimizer$optimize(instance)

  # Returns best scoring evaluation
  instance$result

  # Allows access of data.table of full path of all evaluations
  as.data.table(instance$archive$data)
}
```

Description

OptimizerDesignPoints class that implements optimization w.r.t. fixed design points. We simply search over a set of points fully specified by the user. The points in the design are evaluated in order as given.

In order to support general termination criteria and parallelization, we evaluate points in a batch-fashion of size `batch_size`. Larger batches mean we can parallelize more, smaller batches imply a more fine-grained checking of termination criteria.

Dictionary

This [Optimizer](#) can be instantiated via the [dictionary mlr_optimizers](#) or with the associated sugar function `opt()`:

```
mlr_optimizers$get("design_points")
opt("design_points")
```

Parameters

`batch_size` integer(1)
Maximum number of configurations to try in a batch.

`design` [data.table::data.table](#)
Design points to try in search, one per row.

Progress Bars

`$optimize()` supports progress bars via the package **progressr** combined with a [Terminator](#). Simply wrap the function in `progressr::with_progress()` to enable them. We recommend to use package **progress** as backend; enable with `progressr::handlers("progress")`.

Super class

```
bbotk::Optimizer -> OptimizerDesignPoints
```

Methods**Public methods:**

- [OptimizerDesignPoints\\$new\(\)](#)
- [OptimizerDesignPoints\\$clone\(\)](#)

Method `new()`: Creates a new instance of this R6 class.

Usage:

```
OptimizerDesignPoints$new()
```

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
OptimizerDesignPoints$clone(deep = FALSE)
```

Arguments:

`deep` Whether to make a deep clone.

Examples

```

library(paradox)
library(data.table)

domain = ParamSet$new(list(ParamDbl$new("x", lower = -1, upper = 1)))

search_space = ParamSet$new(list(ParamDbl$new("x", lower = -1, upper = 1)))

codomain = ParamSet$new(list(ParamDbl$new("y", tags = "minimize")))

objective_function = function(xs) {
  list(y = as.numeric(xs)^2)
}

objective = ObjectiveRfun$new(fun = objective_function,
  domain = domain,
  codomain = codomain)
terminator = trm("evals", n_evals = 10)
instance = OptimInstanceSingleCrit$new(
  objective = objective,
  search_space = search_space,
  terminator = terminator)

design = data.table(x = c(0, 1))

optimizer = opt("design_points", design = design)

# Modifies the instance by reference
optimizer$optimize(instance)

# Returns best scoring evaluation
instance$result

# Allows access of data.table of full path of all evaluations
as.data.table(instance$archive)

```

mlr_optimizers_gensa *Optimization via Generalized Simulated Annealing*

Description

OptimizerGenSA class that implements generalized simulated annealing. Calls `GenSA::GenSA()` from package **GenSA**.

Dictionary

This [Optimizer](#) can be instantiated via the [dictionary mlr_optimizers](#) or with the associated sugar function `opt()`:

```
mlr_optimizers$get("gensa")  
opt("gensa")
```

Parameters

```
smooth logical(1)  
temperature numeric(1)  
acceptance.param numeric(1)  
verbose logical(1)  
trace.mat logical(1)
```

For the meaning of the control parameters, see [GenSA::GenSA\(\)](#). Note that we have removed all control parameters which refer to the termination of the algorithm and where our terminators allow to obtain the same behavior.

Progress Bars

`$optimize()` supports progress bars via the package **progressr** combined with a [Terminator](#). Simply wrap the function in `progressr::with_progress()` to enable them. We recommend to use package **progress** as backend; enable with `progressr::handlers("progress")`.

Super class

```
bbotk::Optimizer -> OptimizerGenSA
```

Methods

Public methods:

- [OptimizerGenSA\\$new\(\)](#)
- [OptimizerGenSA\\$clone\(\)](#)

Method `new()`: Creates a new instance of this R6 class.

Usage:

```
OptimizerGenSA$new()
```

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
OptimizerGenSA$clone(deep = FALSE)
```

Arguments:

`deep` Whether to make a deep clone.

Source

Tsallis C, Stariolo DA (1996). “Generalized simulated annealing.” *Physica A: Statistical Mechanics and its Applications*, **233**(1-2), 395–406. doi: [10.1016/s03784371\(96\)002713](https://doi.org/10.1016/s03784371(96)002713).

Xiang Y, Gubian S, Suomela B, Hoeng J (2013). “Generalized Simulated Annealing for Global Optimization: The GenSA Package.” *The R Journal*, **5**(1), 13. doi: [10.32614/rj2013002](https://doi.org/10.32614/rj2013002).

Examples

```

if(requireNamespace("GenSA")) {
  library(paradox)

  domain = ParamSet$new(list(ParamDbl$new("x", lower = -1, upper = 1)))

  search_space = ParamSet$new(list(ParamDbl$new("x", lower = -1, upper = 1)))

  codomain = ParamSet$new(list(ParamDbl$new("y", tags = "minimize")))

  objective_function = function(xs) {
    list(y = as.numeric(xs)^2)
  }

  objective = ObjectiveRfun$new(fun = objective_function,
                                domain = domain,
                                codomain = codomain)

  terminator = trm("evals", n_evals = 10)
  instance = OptimInstanceSingleCrit$new(
    objective = objective,
    search_space = search_space,
    terminator = terminator)

  optimizer = opt("cmaes")

  # Modifies the instance by reference
  optimizer$optimize(instance)

  # Returns best scoring evaluation
  instance$result

  # Allows access of data.table of full path of all evaluations
  as.data.table(instance$archive$data)
}

```

mlr_optimizers_grid_search

Optimization via Grid Search

Description

OptimizerGridSearch class that implements grid search. The grid is constructed as a Cartesian product over discretized values per parameter, see [paradox::generate_design_grid\(\)](#). The points of the grid are evaluated in a random order.

In order to support general termination criteria and parallelization, we evaluate points in a batch-fashion of size `batch_size`. Larger batches mean we can parallelize more, smaller batches imply a more fine-grained checking of termination criteria.

Dictionary

This [Optimizer](#) can be instantiated via the [dictionary mlr_optimizers](#) or with the associated sugar function `opt()`:

```
mlr_optimizers$get("grid_search")
opt("grid_search")
```

Parameters

`resolution` `integer(1)`
Resolution of the grid, see [paradox::generate_design_grid\(\)](#).

`param_resolutions` `named integer()`
Resolution per parameter, named by parameter ID, see [paradox::generate_design_grid\(\)](#).

`batch_size` `integer(1)`
Maximum number of points to try in a batch.

Progress Bars

`$optimize()` supports progress bars via the package [progressr](#) combined with a [Terminator](#). Simply wrap the function in `progressr::with_progress()` to enable them. We recommend to use package [progress](#) as backend; enable with `progressr::handlers("progress")`.

Super class

```
bbotk::Optimizer -> OptimizerGridSearch
```

Methods

Public methods:

- [OptimizerGridSearch\\$new\(\)](#)
- [OptimizerGridSearch\\$clone\(\)](#)

Method `new()`: Creates a new instance of this [R6](#) class.

Usage:

```
OptimizerGridSearch$new()
```

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
OptimizerGridSearch$clone(deep = FALSE)
```

Arguments:

`deep` Whether to make a deep clone.

Examples

```

library(paradox)

domain = ParamSet$new(list(ParamDbl$new("x", lower = -1, upper = 1)))

search_space = ParamSet$new(list(ParamDbl$new("x", lower = -1, upper = 1)))

codomain = ParamSet$new(list(ParamDbl$new("y", tags = "minimize")))

objective_function = function(xs) {
  list(y = as.numeric(xs)^2)
}

objective = ObjectiveRfun$new(fun = objective_function,
                             domain = domain,
                             codomain = codomain)

terminator = trm("evals", n_evals = 10)
instance = OptimInstanceSingleCrit$new(
  objective = objective,
  search_space = search_space,
  terminator = terminator)

optimizer = opt("grid_search")

# Modifies the instance by reference
optimizer$optimize(instance)

# Returns best scoring evaluation
instance$result

# Allows access of data.table of full path of all evaluations
as.data.table(instance$archive$data)

```

mlr_optimizers_nloptr *Optimization via Non-linear Optimization*

Description

OptimizerNloptr class that implements non-linear optimization. Calls `nloptr::nloptr()` from package **nloptr**.

Parameters

```

algorithm character(1)
eval_g_ineq function()
xtol_rel numeric(1)
xtol_abs numeric(1)

```



```
ftol_rel numeric(1)
```

```
ftol_abs numeric(1)
```

```
start_values character(1)
```

Create random start values or based on center of search space? In the latter case, it is the center of the parameters before a trafo is applied.

For the meaning of the control parameters, see `nloptr::nloptr()` and `nloptr::nloptr.print.options()`.

The termination conditions `stopval`, `maxtime` and `maxeval` of `nloptr::nloptr()` are deactivated and replaced by the `Terminator` subclasses. The `x` and function value tolerance termination conditions (`xtol_rel = 10^-4`, `xtol_abs = rep(0.0, length(x0))`, `ftol_rel = 0.0` and `ftol_abs = 0.0`) are still available and implemented with their package defaults. To deactivate these conditions, set them to `-1`.

Progress Bars

`$optimize()` supports progress bars via the package `progressr` combined with a `Terminator`. Simply wrap the function in `progressr::with_progress()` to enable them. We recommend to use package `progress` as backend; enable with `progressr::handlers("progress")`.

Super class

```
bbotk::Optimizer -> OptimizerNLOptr
```

Methods

Public methods:

- `OptimizerNLOptr$new()`
- `OptimizerNLOptr$clone()`

Method `new()`: Creates a new instance of this R6 class.

Usage:

```
OptimizerNLOptr$new()
```

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
OptimizerNLOptr$clone(deep = FALSE)
```

Arguments:

`deep` Whether to make a deep clone.

Source

Johnson, G S (2020). "The NLOpt nonlinear-optimization package." <https://github.com/stevengj/nlopt>.

Examples

```

if(requireNamespace("nloptr")) {
  library(paradox)

  domain = ParamSet$new(list(ParamDbl$new("x", lower = -1, upper = 1)))

  search_space = ParamSet$new(list(ParamDbl$new("x", lower = -1, upper = 1)))

  codomain = ParamSet$new(list(ParamDbl$new("y", tags = "minimize")))

  objective_function = function(xs) {
    list(y = as.numeric(xs)^2)
  }

  objective = ObjectiveRfun$new(fun = objective_function,
    domain = domain,
    codomain = codomain)

  # We use the internal termination criterion xtol_rel
  terminator = trm("none")
  instance = OptimInstanceSingleCrit$new(
    objective = objective,
    search_space = search_space,
    terminator = terminator)

  optimizer = opt("nloptr", algorithm = "NLOPT_LN_BOBYQA")

  # Modifies the instance by reference
  optimizer$optimize(instance)

  # Returns best scoring evaluation
  instance$result

  # Allows access of data.table of full path of all evaluations
  as.data.table(instance$archive)
}

```

mlr_optimizers_random_search

Optimization via Random Search

Description

OptimizerRandomSearch class that implements a simple Random Search.

In order to support general termination criteria and parallelization, we evaluate points in a batch-fashion of size `batch_size`. Larger batches mean we can parallelize more, smaller batches imply a more fine-grained checking of termination criteria.

Dictionary

This [Optimizer](#) can be instantiated via the [dictionary mlr_optimizers](#) or with the associated sugar function `opt()`:

```
mlr_optimizers$get("random_search")
opt("random_search")
```

Parameters

`batch_size` `integer(1)`
Maximum number of points to try in a batch.

Progress Bars

`$optimize()` supports progress bars via the package **progressr** combined with a [Terminator](#). Simply wrap the function in `progressr::with_progress()` to enable them. We recommend to use package **progress** as backend; enable with `progressr::handlers("progress")`.

Super class

```
bbotk::Optimizer -> OptimizerRandomSearch
```

Methods

Public methods:

- [OptimizerRandomSearch\\$new\(\)](#)
- [OptimizerRandomSearch\\$clone\(\)](#)

Method `new()`: Creates a new instance of this [R6](#) class.

Usage:

```
OptimizerRandomSearch$new()
```

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
OptimizerRandomSearch$clone(deep = FALSE)
```

Arguments:

`deep` Whether to make a deep clone.

Source

Bergstra J, Bengio Y (2012). “Random Search for Hyper-Parameter Optimization.” *Journal of Machine Learning Research*, **13**(10), 281–305. <https://jmlr.csail.mit.edu/papers/v13/bergstra12a.html>.

Examples

```

library(paradox)

domain = ParamSet$new(list(ParamDbf$new("x", lower = -1, upper = 1)))

search_space = ParamSet$new(list(ParamDbf$new("x", lower = -1, upper = 1)))

codomain = ParamSet$new(list(ParamDbf$new("y", tags = "minimize")))

objective_function = function(xs) {
  list(y = as.numeric(xs)^2)
}

objective = ObjectiveRfun$new(fun = objective_function,
                             domain = domain,
                             codomain = codomain)

terminator = trm("evals", n_evals = 10)
instance = OptimInstanceSingleCrit$new(
  objective = objective,
  search_space = search_space,
  terminator = terminator)

optimizer = opt("random_search")

# Modifies the instance by reference
optimizer$optimize(instance)

# Returns best scoring evaluation
instance$result

# Allows access of data.table of full path of all evaluations
as.data.table(instance$archive$data)

```

mlr_terminators

Dictionary of Terminators

Description

A simple [mlr3misc::Dictionary](#) storing objects of class [Terminator](#). Each terminator has an associated help page, see `mlr_terminators_[id]`.

This dictionary can get populated with additional terminators by add-on packages.

For a more convenient way to retrieve and construct terminator, see [trm\(\)/trms\(\)](#).

Format

[R6::R6Class](#) object inheriting from [mlr3misc::Dictionary](#).

Methods

See [mlr3misc::Dictionary](#).

See Also

Sugar functions: [trm\(\)](#), [trms\(\)](#)

Other Terminator: [Terminator](#), [mlr_terminators_clock_time](#), [mlr_terminators_combo](#), [mlr_terminators_evals](#), [mlr_terminators_none](#), [mlr_terminators_perf_reached](#), [mlr_terminators_run_time](#), [mlr_terminators_stagnation](#), [mlr_terminators_stagnation](#)

Examples

```
trm("evals", n_evals = 10)
```

```
mlr_terminators_clock_time
```

Terminator that stops according to the clock time

Description

Class to terminate the optimization after a fixed time point has been reached (as reported by [Sys.time\(\)](#)).

Dictionary

This [Terminator](#) can be instantiated via the [dictionary mlr_terminators](#) or with the associated sugar function [trm\(\)](#):

```
mlr_terminators$get("clock_time")
trm("clock_time")
```

Parameters

`stop_time` `POSIXct(1)`
Terminator stops after this point in time.

Super class

[bbotk::Terminator](#) -> TerminatorClockTime

Methods**Public methods:**

- [TerminatorClockTime\\$new\(\)](#)
- [TerminatorClockTime\\$is_terminated\(\)](#)
- [TerminatorClockTime\\$clone\(\)](#)

Method `new()`: Creates a new instance of this [R6](#) class.

Usage:

```
TerminatorClockTime$new()
```

Method `is_terminated()`: Is TRUE iff the termination criterion is positive, and FALSE otherwise.

Usage:

```
TerminatorClockTime$is_terminated(archive)
```

Arguments:

archive ([Archive](#)).

Returns: logical(1).

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
TerminatorClockTime$clone(deep = FALSE)
```

Arguments:

deep Whether to make a deep clone.

See Also

Other Terminator: [Terminator](#), [mlr_terminators_combo](#), [mlr_terminators_evals](#), [mlr_terminators_none](#), [mlr_terminators_perf_reached](#), [mlr_terminators_run_time](#), [mlr_terminators_stagnation_batch](#), [mlr_terminators_stagnation](#), [mlr_terminators](#)

Examples

```
stop_time = as.POSIXct("2030-01-01 00:00:00")
trm("clock_time", stop_time = stop_time)
```

mlr_terminators_combo *Combine Terminators*

Description

This class takes multiple [Terminator](#)s and terminates as soon as one or all of the included terminators are positive.

Dictionary

This [Terminator](#) can be instantiated via the [dictionary mlr_terminators](#) or with the associated sugar function `trm()`:

```
mlr_terminators$get("combo")
trm("combo")
```

Parameters

any logical(1)

Terminate iff any included terminator is positive? (not all), default is TRUE.

Super class

`bbotk::Terminator` -> TerminatorCombo

Public fields

terminators (list())

List of objects of class `Terminator`.

Methods**Public methods:**

- `TerminatorCombo$new()`
- `TerminatorCombo$is_terminated()`
- `TerminatorCombo$print()`
- `TerminatorCombo$remaining_time()`
- `TerminatorCombo$status_long()`
- `TerminatorCombo$clone()`

Method `new()`: Creates a new instance of this `R6` class.

Usage:

```
TerminatorCombo$new(terminators = list(TerminatorNone$new()))
```

Arguments:

terminators (list())

List of objects of class `Terminator`.

Method `is_terminated()`: Is TRUE iff the termination criterion is positive, and FALSE otherwise.

Usage:

```
TerminatorCombo$is_terminated(archive)
```

Arguments:

archive (`Archive`).

Returns: logical(1).

Method `print()`: Printer.

Usage:

```
TerminatorCombo$print(...)
```

Arguments:

... (ignored).

Method `remaining_time()`: Returns the remaining runtime in seconds. If `any = TRUE`, the remaining runtime is determined by the time-based terminator with the shortest time remaining. If non-time-based terminators are used and `any = FALSE`, the the remaining runtime is always `Inf`.

Usage:

```
TerminatorCombo$remaining_time(archive)
```

Arguments:

`archive` ([Archive](#)).

Returns: `integer(1)`.

Method `status_long()`: Returns `max_steps` and `current_steps` for each terminator.

Usage:

```
TerminatorCombo$status_long(archive)
```

Arguments:

`archive` ([Archive](#)).

Returns: `data.table::data.table`.

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
TerminatorCombo$clone(deep = FALSE)
```

Arguments:

`deep` Whether to make a deep clone.

See Also

Other Terminator: [Terminator](#), [mlr_terminators_clock_time](#), [mlr_terminators_evals](#), [mlr_terminators_none](#), [mlr_terminators_perf_reached](#), [mlr_terminators_run_time](#), [mlr_terminators_stagnation_batch](#), [mlr_terminators_stagnation](#), [mlr_terminators](#)

Examples

```
trm("combo",
  list(trm("clock_time", stop_time = Sys.time() + 60),
    trm("evals", n_evals = 10)), any = FALSE
)
```

`mlr_terminators_evals` *Terminator that stops after a number of evaluations*

Description

Class to terminate the optimization depending on the number of evaluations. An evaluation is defined by one resampling of a parameter value.

Dictionary

This [Terminator](#) can be instantiated via the [dictionary mlr_terminators](#) or with the associated sugar function `trm()`:

```
mlr_terminators$get("evals")
trm("evals")
```

Parameters

`n_evals` integer(1)
Number of allowed evaluations, default is 100L.

Super class

`bbotk::Terminator` -> TerminatorEvals

Methods**Public methods:**

- [TerminatorEvals\\$new\(\)](#)
- [TerminatorEvals\\$is_terminated\(\)](#)
- [TerminatorEvals\\$clone\(\)](#)

Method `new()`: Creates a new instance of this [R6](#) class.

Usage:

```
TerminatorEvals$new()
```

Method `is_terminated()`: Is TRUE iff the termination criterion is positive, and FALSE otherwise.

Usage:

```
TerminatorEvals$is_terminated(archive)
```

Arguments:

`archive` ([Archive](#)).

Returns: logical(1).

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
TerminatorEvals$clone(deep = FALSE)
```

Arguments:

`deep` Whether to make a deep clone.

See Also

Other Terminator: [Terminator](#), [mlr_terminators_clock_time](#), [mlr_terminators_combo](#), [mlr_terminators_none](#), [mlr_terminators_perf_reached](#), [mlr_terminators_run_time](#), [mlr_terminators_stagnation_batch](#), [mlr_terminators_stagnation](#), [mlr_terminators](#)

Examples

```
TerminatorEvals$new()
trm("evals", n_evals = 5)
```

```
mlr_terminators_none Terminator that never stops.
```

Description

Mainly useful for optimization algorithms where the stopping is inherently controlled by the algorithm itself (e.g. [OptimizerGridSearch](#)).

Dictionary

This [Terminator](#) can be instantiated via the [dictionary mlr_terminators](#) or with the associated sugar function `trm()`:

```
mlr_terminators$get("none")
trm("none")
```

Super class

```
bbotk::Terminator -> TerminatorNone
```

Methods**Public methods:**

- [TerminatorNone\\$new\(\)](#)
- [TerminatorNone\\$is_terminated\(\)](#)
- [TerminatorNone\\$clone\(\)](#)

Method `new()`: Creates a new instance of this [R6](#) class.

Usage:

```
TerminatorNone$new()
```

Method `is_terminated()`: Is TRUE iff the termination criterion is positive, and FALSE otherwise.

Usage:

```
TerminatorNone$is_terminated(archive)
```

Arguments:

archive ([Archive](#)).

Returns: logical(1).

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
TerminatorNone$clone(deep = FALSE)
```

Arguments:

deep Whether to make a deep clone.

See Also

Other Terminator: [Terminator](#), [mlr_terminators_clock_time](#), [mlr_terminators_combo](#), [mlr_terminators_evals](#), [mlr_terminators_perf_reached](#), [mlr_terminators_run_time](#), [mlr_terminators_stagnation_batch](#), [mlr_terminators_stagnation](#), [mlr_terminators](#)

mlr_terminators_perf_reached

Terminator that stops when a performance level has been reached

Description

Class to terminate the optimization after a performance level has been hit.

Dictionary

This [Terminator](#) can be instantiated via the [dictionary mlr_terminators](#) or with the associated sugar function [trm\(\)](#):

```
mlr_terminators$get("perf_reached")
trm("perf_reached")
```

Parameters

level numeric(1)

Performance level that needs to be reached, default is 0. Terminates if the performance exceeds (respective measure has to be maximized) or falls below (respective measure has to be minimized) this value.

Super class

[bbotk::Terminator](#) -> TerminatorPerfReached

Methods**Public methods:**

- [TerminatorPerfReached\\$new\(\)](#)
- [TerminatorPerfReached\\$is_terminated\(\)](#)
- [TerminatorPerfReached\\$clone\(\)](#)

Method [new\(\)](#): Creates a new instance of this [R6](#) class.

Usage:

```
TerminatorPerfReached$new()
```

Method [is_terminated\(\)](#): Is TRUE iff the termination criterion is positive, and FALSE otherwise.

Usage:

TerminatorPerfReached\$is_terminated(archive)

Arguments:

archive ([Archive](#)).

Returns: logical(1).

Method clone(): The objects of this class are cloneable with this method.

Usage:

TerminatorPerfReached\$clone(deep = FALSE)

Arguments:

deep Whether to make a deep clone.

See Also

Other Terminator: [Terminator](#), [mlr_terminators_clock_time](#), [mlr_terminators_combo](#), [mlr_terminators_evals](#), [mlr_terminators_none](#), [mlr_terminators_run_time](#), [mlr_terminators_stagnation_batch](#), [mlr_terminators_stagnation](#), [mlr_terminators](#)

Examples

```
TerminatorPerfReached$new()
trm("perf_reached")
```

mlr_terminators_run_time

Terminator that stops according to the run time

Description

Class to terminate the optimization after the optimization process took a number of seconds on the clock.

Dictionary

This [Terminator](#) can be instantiated via the [dictionary mlr_terminators](#) or with the associated sugar function [trm\(\)](#):

```
mlr_terminators$get("run_time")
trm("run_time")
```

Parameters

secs numeric(1)
Maximum allowed time, in seconds, default is 100.

Super class

[bbotk::Terminator](#) -> TerminatorRunTime

Methods

Public methods:

- [TerminatorRunTime\\$new\(\)](#)
- [TerminatorRunTime\\$is_terminated\(\)](#)
- [TerminatorRunTime\\$clone\(\)](#)

Method `new()`: Creates a new instance of this [R6](#) class.

Usage:

```
TerminatorRunTime$new()
```

Method `is_terminated()`: Is TRUE iff the termination criterion is positive, and FALSE otherwise.

Usage:

```
TerminatorRunTime$is_terminated(archive)
```

Arguments:

archive ([Archive](#)).

Returns: `logical(1)`.

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
TerminatorRunTime$clone(deep = FALSE)
```

Arguments:

deep Whether to make a deep clone.

See Also

Other Terminator: [Terminator](#), [mlr_terminators_clock_time](#), [mlr_terminators_combo](#), [mlr_terminators_evals](#), [mlr_terminators_none](#), [mlr_terminators_perf_reached](#), [mlr_terminators_stagnation_batch](#), [mlr_terminators_stagnation](#), [mlr_terminators](#)

Examples

```
trm("run_time", secs = 1800)
```

mlr_terminators_stagnation

Terminator that stops when optimization does not improve

Description

Class to terminate the optimization after the performance stagnates, i.e. does not improve more than threshold over the last `iters` iterations.

Dictionary

This [Terminator](#) can be instantiated via the [dictionary mlr_terminators](#) or with the associated sugar function `trm()`:

```
mlr_terminators$get("stagnation")
trm("stagnation")
```

Parameters

`iters` integer(1)
Number of iterations to evaluate the performance improvement on, default is 10.

`threshold` numeric(1)
If the improvement is less than threshold, optimization is stopped, default is 0.

Super class

`bbotk::Terminator` -> TerminatorStagnation

Methods**Public methods:**

- [TerminatorStagnation\\$new\(\)](#)
- [TerminatorStagnation\\$is_terminated\(\)](#)
- [TerminatorStagnation\\$clone\(\)](#)

Method `new()`: Creates a new instance of this [R6](#) class.

Usage:

```
TerminatorStagnation$new()
```

Method `is_terminated()`: Is TRUE iff the termination criterion is positive, and FALSE otherwise.

Usage:

```
TerminatorStagnation$is_terminated(archive)
```

Arguments:

`archive` ([Archive](#)).

Returns: logical(1).

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
TerminatorStagnation$clone(deep = FALSE)
```

Arguments:

`deep` Whether to make a deep clone.

See Also

Other Terminator: [Terminator](#), [mlr_terminators_clock_time](#), [mlr_terminators_combo](#), [mlr_terminators_evals](#), [mlr_terminators_none](#), [mlr_terminators_perf_reached](#), [mlr_terminators_run_time](#), [mlr_terminators_stagnation_batch](#), [mlr_terminators](#)

Examples

```
TerminatorStagnation$new()
trm("stagnation", iters = 5, threshold = 1e-5)
```

```
mlr_terminators_stagnation_batch
```

Terminator that stops when optimization does not improve

Description

Class to terminate the optimization after the performance stagnates, i.e. does not improve more than threshold over the last n batches.

Dictionary

This [Terminator](#) can be instantiated via the [dictionary mlr_terminators](#) or with the associated sugar function [trm\(\)](#):

```
mlr_terminators$get("stagnation_batch")
trm("stagnation_batch")
```

Parameters

n integer(1)

Number of batches to evaluate the performance improvement on, default is 1.

threshold numeric(1)

If the improvement is less than threshold, optimization is stopped, default is 0.

Super class

[bbotk::Terminator](#) -> TerminatorStagnationBatch

Methods**Public methods:**

- [TerminatorStagnationBatch\\$new\(\)](#)
- [TerminatorStagnationBatch\\$is_terminated\(\)](#)
- [TerminatorStagnationBatch\\$clone\(\)](#)

Method [new\(\)](#): Creates a new instance of this [R6](#) class.

Usage:

```
TerminatorStagnationBatch$new()
```

Method `is_terminated()`: Is TRUE iff the termination criterion is positive, and FALSE otherwise.

Usage:

```
TerminatorStagnationBatch$is_terminated(archive)
```

Arguments:

archive ([Archive](#)).

Returns: logical(1).

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
TerminatorStagnationBatch$clone(deep = FALSE)
```

Arguments:

deep Whether to make a deep clone.

See Also

Other Terminator: [Terminator](#), [mlr_terminators_clock_time](#), [mlr_terminators_combo](#), [mlr_terminators_evals](#), [mlr_terminators_none](#), [mlr_terminators_perf_reached](#), [mlr_terminators_run_time](#), [mlr_terminators_stagnation](#), [mlr_terminators](#)

Examples

```
TerminatorStagnationBatch$new()
trm("stagnation_batch", n = 1, threshold = 1e-5)
```

Objective

Objective function with domain and co-domain

Description

Describes a black-box objective function that maps an arbitrary domain to a numerical codomain.

Technical details

Objective objects can have the following properties: "noisy", "deterministic", "single-crit" and "multi-crit".

Public fields

id (character(1)).

properties (character()).

domain ([paradox::ParamSet](#))
Specifies domain of function, hence its input parameters, their types and ranges.

codomain ([paradox::ParamSet](#))
Specifies codomain of function, hence its feasible values.

constants ([paradox::ParamSet](#)).
Changeable constants or parameters that are not subject to tuning can be stored and accessed here.

check_values (logical(1))

Active bindings

xdim (integer(1))
Dimension of domain.

ydim (integer(1))
Dimension of codomain.

Methods**Public methods:**

- [Objective\\$new\(\)](#)
- [Objective\\$format\(\)](#)
- [Objective\\$print\(\)](#)
- [Objective\\$eval\(\)](#)
- [Objective\\$eval_many\(\)](#)
- [Objective\\$eval_dt\(\)](#)
- [Objective\\$clone\(\)](#)

Method `new()`: Creates a new instance of this [R6](#) class.

Usage:

```
Objective$new(
  id = "f",
  properties = character(),
  domain,
  codomain = ParamSet$new(list(ParamDb1$new("y", tags = "minimize"))),
  constants = ParamSet$new(),
  check_values = TRUE
)
```

Arguments:

id (character(1)).

properties (character()).

domain ([paradox::ParamSet](#))

Specifies domain of function. The [paradox::ParamSet](#) should describe all possible input parameters of the objective function. This includes their id, their types and the possible range.

codomain ([paradox::ParamSet](#))

Specifies codomain of function. Most importantly the tags of each output "Parameter" define whether it should be minimized or maximized. The default is to minimize each component.

constants ([paradox::ParamSet](#))

Changeable constants or parameters that are not subject to tuning can be stored and accessed here.

check_values (logical(1))

Should points before the evaluation and the results be checked for validity?

Method format(): Helper for print outputs.

Usage:

Objective\$format()

Returns: character().

Method print(): Print method.

Usage:

Objective\$print()

Returns: character().

Method eval(): Evaluates a single input value on the objective function. If check_values = TRUE, the validity of the point as well as the validity of the result is checked.

Usage:

Objective\$eval(xs)

Arguments:

xs (list())

A list that contains a single x value, e.g. list(x1 = 1, x2 = 2).

Returns: list() that contains the result of the evaluation, e.g. list(y = 1). The list can also contain additional *named* entries that will be stored in the archive if called through the [OptimInstance](#). These extra entries are referred to as *extras*.

Method eval_many(): Evaluates multiple input values on the objective function. If check_values = TRUE, the validity of the points as well as the validity of the results are checked. *bbotk* does not take care of parallelization. If the function should make use of parallel computing, it has to be implemented by deriving from this class and overwriting this function.

Usage:

Objective\$eval_many(xss)

Arguments:

xss (list())

A list of lists that contains multiple x values, e.g. list(list(x1 = 1, x2 = 2), list(x1 = 3, x2 = 4)).

Returns: `data.table::data.table()` that contains one y-column for single-criteria functions and multiple y-columns for multi-criteria functions, e.g. `data.table(y = 1:2)` or `data.table(y1 = 1:2, y2 = 3:4)`. It may also contain additional columns that will be stored in the archive if called through the [OptimInstance](#). These extra columns are referred to as *extras*.

Method `eval_dt()`: Evaluates multiple input values on the objective function

Usage:

```
Objective$eval_dt(xdt)
```

Arguments:

`xdt` (`data.table::data.table()`)

Set of untransformed points / points from the *search space*. One point per row, e.g. `data.table(x1 = c(1, 3), x2 = c(2, 4))`. Column names have to match ids of the `search_space`. However, `xdt` can contain additional columns.

Returns: `data.table::data.table()` that contains one y-column for single-criteria functions and multiple y-columns for multi-criteria functions, e.g. `data.table(y = 1:2)` or `data.table(y1 = 1:2, y2 = 3:4)`.

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
Objective$clone(deep = FALSE)
```

Arguments:

`deep` Whether to make a deep clone.

ObjectiveRFun

Objective interface with custom R function

Description

Objective interface where the user can pass a custom R function that expects a list as input.

Super class

`bbotk::Objective` -> ObjectiveRFun

Active bindings

`fun` (function)
Objective function.

Methods

Public methods:

- [ObjectiveRFun\\$new\(\)](#)
- [ObjectiveRFun\\$eval\(\)](#)
- [ObjectiveRFun\\$clone\(\)](#)

Method `new()`: Creates a new instance of this [R6](#) class.

Usage:

```
ObjectiveRFun$new(
  fun,
  domain,
  codomain = NULL,
  id = "function",
  properties = character(),
  constants = ParamSet$new(),
  check_values = TRUE
)
```

Arguments:

`fun` (function)

R function that encodes objective and expects a list with the input for a single point (e.g. `list(x1 = 1, x2 = 2)`) and returns the result either as a numeric vector or a list (e.g. `list(y = 3)`).

`domain` ([paradox::ParamSet](#))

Specifies domain of function. The [paradox::ParamSet](#) should describe all possible input parameters of the objective function. This includes their id, their types and the possible range.

`codomain` ([paradox::ParamSet](#))

Specifies codomain of function. Most importantly the tags of each output "Parameter" define whether it should be minimized or maximized. The default is to minimize each component.

`id` (`character(1)`).

`properties` (`character()`).

`constants` ([paradox::ParamSet](#))

Changeable constants or parameters that are not subject to tuning can be stored and accessed here.

`check_values` (`logical(1)`)

Should points before the evaluation and the results be checked for validity?

Method `eval()`: Evaluates input value(s) on the objective function. Calls the R function supplied by the user.

Usage:

```
ObjectiveRFun$eval(xs)
```

Arguments:

`xs` Input values.

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
ObjectiveRFuncDt$clone(deep = FALSE)
```

Arguments:

`deep` Whether to make a deep clone.

Examples

```
library(paradox)
# Define objective function
fun = function(xs) {
  - (xs[[1]] - 2)^2 - (xs[[2]] + 3)^2 + 10
}

# Set domain
domain = ParamSet$new(list(
  ParamDbf$new("x1", -10, 10),
  ParamDbf$new("x2", -5, 5)
))

# Set codomain
codomain = ParamSet$new(list(
  ParamDbf$new("y", tags = "maximize")
))

# Create Objective object
obfun = ObjectiveRFuncDt$new(
  fun = fun,
  domain = domain,
  codomain = codomain,
  properties = "deterministic"
)
```

ObjectiveRFuncDt

Objective interface for basic R functions.

Description

Objective interface where user can pass an R function that works on an `data.table()`.

Super class

`bbotk::Objective` -> ObjectiveRFuncDt

Active bindings

`fun` (function)
Objective function.

Methods

Public methods:

- [ObjectiveRFuncDt\\$new\(\)](#)
- [ObjectiveRFuncDt\\$eval_many\(\)](#)
- [ObjectiveRFuncDt\\$eval_dt\(\)](#)
- [ObjectiveRFuncDt\\$clone\(\)](#)

Method `new()`: Creates a new instance of this R6 class.

Usage:

```
ObjectiveRFuncDt$new(
  fun,
  domain,
  codomain = NULL,
  id = "function",
  properties = character(),
  constants = ParamSet$new(),
  check_values = TRUE
)
```

Arguments:

`fun` (function)

R function that encodes objective and expects an `data.table()` as input whereas each point is represented by one row.

`domain` ([paradox::ParamSet](#))

Specifies domain of function. The [paradox::ParamSet](#) should describe all possible input parameters of the objective function. This includes their id, their types and the possible range.

`codomain` ([paradox::ParamSet](#))

Specifies codomain of function. Most importantly the tags of each output "Parameter" define whether it should be minimized or maximized. The default is to minimize each component.

`id` (`character(1)`).

`properties` (`character()`).

`constants` ([paradox::ParamSet](#))

Changeable constants or parameters that are not subject to tuning can be stored and accessed here.

`check_values` (`logical(1)`)

Should points before the evaluation and the results be checked for validity?

Method `eval_many()`: Evaluates multiple input values received as a list, converted to a `data.table()` on the objective function.

Usage:

```
ObjectiveRFuncDt$eval_many(xss)
```

Arguments:

`xss` (`list()`)

A list of lists that contains multiple x values, e.g. `list(list(x1 = 1, x2 = 2), list(x1 = 3, x2 = 4))`.

Returns: `data.table::data.table()` that contains one y-column for single-criteria functions and multiple y-columns for multi-criteria functions, e.g. `data.table(y = 1:2)` or `data.table(y1 = 1:2, y2 = 3:4)`.

Method `eval_dt()`: Evaluates multiple input values on the objective function supplied by the user.

Usage:

```
ObjectiveRFunDt$eval_dt(xdt)
```

Arguments:

`xdt` (`data.table::data.table()`)

Set of untransformed points / points from the *search space*. One point per row, e.g. `data.table(x1 = c(1, 3), x2 = c(2, 4))`. Column names have to match ids of the `search_space`. However, `xdt` can contain additional columns.

Returns: `data.table::data.table()` that contains one y-column for single-criteria functions and multiple y-columns for multi-criteria functions, e.g. `data.table(y = 1:2)` or `data.table(y1 = 1:2, y2 = 3:4)`.

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
ObjectiveRFunDt$clone(deep = FALSE)
```

Arguments:

`deep` Whether to make a deep clone.

Description

This function complements `mlr_optimizers` with functions in the spirit of `mlr_sugar` from `mlr3`.

Usage

```
opt(.key, ...)
```

```
opts(.keys, ...)
```

Arguments

<code>.key</code>	(<code>character(1)</code>) Key passed to the respective <code>dictionary</code> to retrieve the object.
<code>...</code>	(<code>named list()</code>) Named arguments passed to the constructor, to be set as parameters in the <code>paradox::ParamSet</code> , or to be set as public field. See <code>mlr3misc::dictionary_sugar_get()</code> for more details.
<code>.keys</code>	(<code>character()</code>) Keys passed to the respective <code>dictionary</code> to retrieve multiple objects.

Value

- [Optimizer](#) for `opt()`.
- list of [Optimizer](#) for `opts()`.

Examples

```
opt("random_search", batch_size = 10)
```

 OptimInstance

Optimization Instance with budget and archive

Description

Abstract base class.

Technical details

The [Optimizer](#) writes the final result to the `.result` field by using the `$assign_result()` method. `.result` stores a [data.table::data.table](#) consisting of x values in the *search space*, (transformed) x values in the *domain space* and y values in the *codomain space* of the [Objective](#). The user can access the results with active bindings (see below).

Public fields

`objective` ([Objective](#)).

`search_space` ([paradox::ParamSet](#)).

`terminator` ([Terminator](#)).

`is_terminated` (`logical(1)`).

`archive` ([Archive](#)).

`progressor` (`progressor()`)
Stores progressor function.

`objective_multiplier` (`integer()`).

Active bindings

`result` ([data.table::data.table](#))
Get result

`result_x_search_space` ([data.table::data.table](#))
 x part of the result in the *search space*.

`result_x_domain` (`list()`)
(transformed) x part of the result in the *domain space* of the objective.

`result_y` (`numeric()`)
Optimal outcome.

Methods**Public methods:**

- `OptimInstance$new()`
- `OptimInstance$format()`
- `OptimInstance$print()`
- `OptimInstance$eval_batch()`
- `OptimInstance$assign_result()`
- `OptimInstance$objective_function()`
- `OptimInstance$clone()`

Method `new()`: Creates a new instance of this R6 class.

Usage:

```
OptimInstance$new(  
  objective,  
  search_space = NULL,  
  terminator,  
  keep_evals = "all",  
  check_values = TRUE  
)
```

Arguments:

`objective` (**Objective**).

`search_space` (**paradox::ParamSet**)

Specifies the search space for the **Optimizer**. The **paradox::ParamSet** describes either a subset of the domain of the **Objective** or it describes a set of parameters together with a trafo function that transforms values from the search space to values of the domain. Depending on the context, this value defaults to the domain of the objective.

`terminator` (**Terminator**).

`keep_evals` (`character(1)`)

Keep all or only best evaluations in archive?

`check_values` (`logical(1)`)

Should x-values that are added to the archive be checked for validity? Search space that is logged into archive.

Method `format()`: Helper for print outputs.

Usage:

```
OptimInstance$format()
```

Method `print()`: Printer.

Usage:

```
OptimInstance$print(...)
```

Arguments:

... (ignored).

Method `eval_batch()`: Evaluates all input values in `xdt` by calling the [Objective](#). Applies possible transformations to the input values and writes the results to the [Archive](#).

Before each batch-evaluation, the [Terminator](#) is checked, and if it is positive, an exception of class `terminated_error` is raised. This function should be internally called by the [Optimizer](#).

Usage:

```
OptimInstance$eval_batch(xdt)
```

Arguments:

`xdt` (`data.table::data.table()`)

x values as `data.table()` with one point per row. Contains the value in the *search space* of the [OptimInstance](#) object. Can contain additional columns for extra information.

Method `assign_result()`: The [Optimizer](#) object writes the best found point and estimated performance value here. For internal use.

Usage:

```
OptimInstance$assign_result(xdt, y)
```

Arguments:

`xdt` (`data.table::data.table()`)

x values as `data.table()` with one row. Contains the value in the *search space* of the [OptimInstance](#) object. Can contain additional columns for extra information.

`y` (`numeric(1)`)

Optimal outcome.

Method `objective_function()`: Evaluates (untransformed) points of only numeric values. Returns a numeric scalar for single-crit or a numeric vector for multi-crit. The return value(s) are negated if the measure is maximized. Internally, `$eval_batch()` is called with a single row. This function serves as a objective function for optimizers of numeric spaces - which should always be minimized.

Usage:

```
OptimInstance$objective_function(x)
```

Arguments:

`x` (`numeric()`)

Untransformed points.

Returns: Objective value as `numeric(1)`, negated for maximization problems.

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
OptimInstance$clone(deep = FALSE)
```

Arguments:

`deep` Whether to make a deep clone.

`OptimInstanceMultiCrit`*Optimization Instance with budget and archive*

Description

Wraps a multi-criteria [Objective](#) function with extra services for convenient evaluation. Inherits from [OptimInstance](#).

- Automatic storing of results in an [Archive](#) after evaluation.
- Automatic checking for termination. Evaluations of design points are performed in batches. Before a batch is evaluated, the [Terminator](#) is queried for the remaining budget. If the available budget is exhausted, an exception is raised, and no further evaluations can be performed from this point on.

Super class

```
bbotk::OptimInstance -> OptimInstanceMultiCrit
```

Active bindings

```
result_x_domain (list())  
  (transformed) x part of the result in the domain space of the objective.  
result_y (numeric(1))  
  Optimal outcome.
```

Methods

Public methods:

- `OptimInstanceMultiCrit$new()`
- `OptimInstanceMultiCrit$assign_result()`
- `OptimInstanceMultiCrit$clone()`

Method `new()`: Creates a new instance of this [R6](#) class.

Usage:

```
OptimInstanceMultiCrit$new(  
  objective,  
  search_space = NULL,  
  terminator,  
  keep_evals = "all",  
  check_values = TRUE  
)
```

Arguments:

`objective` ([Objective](#)).

search_space ([paradox::ParamSet](#))

Specifies the search space for the [Optimizer](#). The [paradox::ParamSet](#) describes either a subset of the domain of the [Objective](#) or it describes a set of parameters together with a trafo function that transforms values from the search space to values of the domain. Depending on the context, this value defaults to the domain of the objective.

terminator ([Terminator](#))

Multi-criteria terminator.

keep_evals ([character\(1\)](#))

Keep all or only best evaluations in archive?

check_values ([logical\(1\)](#))

Should x-values that are added to the archive be checked for validity? Search space that is logged into archive.

Method `assign_result()`: The [Optimizer](#) object writes the best found points and estimated performance values here (probably the Pareto set / front). For internal use.

Usage:

```
OptimInstanceMultiCrit$assign_result(xdt, ydt)
```

Arguments:

xdt ([data.table::data.table\(\)](#))

Set of untransformed points / points from the *search space*. One point per row, e.g. `data.table(x1 = c(1, 3), x2 = c(2, 4))`. Column names have to match ids of the `search_space`. However, xdt can contain additional columns.

ydt ([numeric\(1\)](#))

Optimal outcomes, e.g. the Pareto front.

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
OptimInstanceMultiCrit$clone(deep = FALSE)
```

Arguments:

deep Whether to make a deep clone.

OptimInstanceSingleCrit

Optimization Instance with budget and archive

Description

Wraps a single-criteria [Objective](#) function with extra services for convenient evaluation. Inherits from [OptimInstance](#).

- Automatic storing of results in an [Archive](#) after evaluation.
- Automatic checking for termination. Evaluations of design points are performed in batches. Before a batch is evaluated, the [Terminator](#) is queried for the remaining budget. If the available budget is exhausted, an exception is raised, and no further evaluations can be performed from this point on.

Super class

`bbotk::OptimInstance` -> `OptimInstanceSingleCrit`

Methods**Public methods:**

- `OptimInstanceSingleCrit$new()`
- `OptimInstanceSingleCrit$assign_result()`
- `OptimInstanceSingleCrit$clone()`

Method `new()`: Creates a new instance of this R6 class.

Usage:

```
OptimInstanceSingleCrit$new(
  objective,
  search_space = NULL,
  terminator,
  keep_evals = "all",
  check_values = TRUE
)
```

Arguments:

`objective` (**Objective**).

`search_space` (**paradox::ParamSet**)

Specifies the search space for the **Optimizer**. The **paradox::ParamSet** describes either a subset of the domain of the **Objective** or it describes a set of parameters together with a trafo function that transforms values from the search space to values of the domain. Depending on the context, this value defaults to the domain of the objective.

`terminator` (**Terminator**).

`keep_evals` (`character(1)`)

Keep all or only best evaluations in archive?

`check_values` (`logical(1)`)

Should x-values that are added to the archive be checked for validity? Search space that is logged into archive.

Method `assign_result()`: The **Optimizer** object writes the best found point and estimated performance value here. For internal use.

Usage:

```
OptimInstanceSingleCrit$assign_result(xdt, y)
```

Arguments:

`xdt` (**data.table::data.table()**)

Set of untransformed points / points from the *search space*. One point per row, e.g. `data.table(x1 = c(1, 3), x2 = c(2, 4))`. Column names have to match ids of the `search_space`. However, `xdt` can contain additional columns.

`y` (`numeric(1)`)

Optimal outcome.

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
OptimInstanceSingleCrit$clone(deep = FALSE)
```

Arguments:

deep Whether to make a deep clone.

Optimizer

Optimizer

Description

Abstract Optimizer class that implements the base functionality each Optimizer subclass must provide. A Optimizer object describes the optimization strategy.

A Optimizer object must write its result to the \$assign_result() method of the [OptimInstance](#) at the end in order to store the best point and its estimated performance vector.

Progress Bars

\$optimize() supports progress bars via the package **progressr** combined with a [Terminator](#). Simply wrap the function in `progressr::with_progress()` to enable them. We recommend to use package **progress** as backend; enable with `progressr::handlers("progress")`.

Public fields

param_set ([paradox::ParamSet](#)).

param_classes ([character\(\)](#)).

properties ([character\(\)](#)).

packages ([character\(\)](#)).

Methods

Public methods:

- [Optimizer\\$new\(\)](#)
- [Optimizer\\$format\(\)](#)
- [Optimizer\\$print\(\)](#)
- [Optimizer\\$optimize\(\)](#)
- [Optimizer\\$clone\(\)](#)

Method new(): Creates a new instance of this [R6](#) class.

Usage:

```
Optimizer$new(param_set, param_classes, properties, packages = character())
```

Arguments:

param_set ([paradox::ParamSet](#)).

param_classes ([character\(\)](#)).

properties ([character\(\)](#)).

packages (character()).

Method format(): Helper for print outputs.

Usage:

Optimizer\$format()

Method print(): Print method.

Usage:

Optimizer\$print()

Returns: (character()).

Method optimize(): Performs the optimization and writes optimization result into [OptimInstance](#). The optimization result is returned but the complete optimization path is stored in [Archive](#) of [OptimInstance](#).

Usage:

Optimizer\$optimize(inst)

Arguments:

inst ([OptimInstance](#)).

Returns: [data.table::data.table](#).

Method clone(): The objects of this class are cloneable with this method.

Usage:

Optimizer\$clone(deep = FALSE)

Arguments:

deep Whether to make a deep clone.

Progressor

Progressor

Description

Wraps `progressr::progressor()` function and stores current progress.

Public fields

progressor (`progressr::progressor()`).

max_steps (`integer(1)`).

current_steps (`integer(1)`).

unit (`character(1)`).

Methods

Public methods:

- [Progressor\\$new\(\)](#)
- [Progressor\\$setup\(\)](#)
- [Progressor\\$update\(\)](#)
- [Progressor\\$clone\(\)](#)

Method `new()`: Creates a new instance of this [R6](#) class.

Usage:

```
Progressor$new()
```

Method `setup()`: Creates `progressr::progressor()`.

Usage:

```
Progressor$setup(terminator, archive)
```

Arguments:

terminator ([Terminator](#)).

archive ([Archive](#)).

Method `update()`: Updates `progressr::progressor()` with current steps.

Usage:

```
Progressor$update(terminator, archive)
```

Arguments:

terminator ([Terminator](#)).

archive ([Archive](#)).

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
Progressor$clone(deep = FALSE)
```

Arguments:

deep Whether to make a deep clone.

Terminator

Abstract Terminator Class

Description

Abstract Terminator class that implements the base functionality each terminator must provide. A terminator is an object that determines when to stop the optimization.

Termination of optimization works as follows:

- Evaluations in a instance are performed in batches.
- Before each batch evaluation, the [Terminator](#) is checked, and if it is positive, we stop.

- The optimization algorithm itself might decide not to produce any more points, or even might decide to do a smaller batch in its last evaluation.

Therefore the following note seems in order: While it is definitely possible to execute a fine-grained control for termination, and for many optimization algorithms we can specify exactly when to stop, it might happen that too few or even too many evaluations are performed, especially if multiple points are evaluated in a single batch (c.f. batch size parameter of many optimization algorithms). So it is advised to check the size of the returned archive, in particular if you are benchmarking multiple optimization algorithms.

Technical details

Terminator subclasses can overwrite `.status()` to support progress bars via the package **progressr**. The method must return the maximum number of steps (`max_steps`) and the currently achieved number of steps (`current_steps`) as a named integer vector.

Public fields

`param_set` [paradox::ParamSet](#)
Set of control parameters for terminator.

`properties` (`character()`)
Set of properties.

`unit` (`character()`)
Unit of steps.

Methods

Public methods:

- [Terminator\\$new\(\)](#)
- [Terminator\\$format\(\)](#)
- [Terminator\\$print\(\)](#)
- [Terminator\\$status\(\)](#)
- [Terminator\\$remaining_time\(\)](#)
- [Terminator\\$clone\(\)](#)

Method `new()`: Creates a new instance of this R6 class.

Usage:

```
Terminator$new(param_set = ParamSet$new(), properties = character())
```

Arguments:

`param_set` ([paradox::ParamSet](#))
Set of control parameters for terminator.

`properties` (`character()`)
Set of properties.

Method `format()`: Helper for print outputs.

Usage:

```
Terminator$format(with_params = FALSE)
```

Arguments:

```
with_params (logical(1))  
    Add parameter values to format string.
```

Method print(): Printer.

Usage:

```
Terminator$print(...)
```

Arguments:

```
... (ignored).
```

Method status(): Returns how many progression steps are made (current_steps) and the amount steps needed for termination (max_steps).

Usage:

```
Terminator$status(archive)
```

Arguments:

```
archive (Archive).
```

Returns: named integer(2).

Method remaining_time(): Returns remaining runtime in seconds. If the terminator is not time-based, the remaining runtime is Inf.

Usage:

```
Terminator$remaining_time(archive)
```

Arguments:

```
archive (Archive).
```

Returns: integer(1).

Method clone(): The objects of this class are cloneable with this method.

Usage:

```
Terminator$clone(deep = FALSE)
```

Arguments:

```
deep Whether to make a deep clone.
```

See Also

Other Terminator: [mlr_terminators_clock_time](#), [mlr_terminators_combo](#), [mlr_terminators_evals](#), [mlr_terminators_none](#), [mlr_terminators_perf_reached](#), [mlr_terminators_run_time](#), [mlr_terminators_stagnation](#), [mlr_terminators_stagnation](#), [mlr_terminators](#)

`trm`*Syntactic Sugar Terminator Construction*

Description

This function complements [mlr_terminators](#) with functions in the spirit of `mlr_sugar` from **mlr3**.

Usage

```
trm(.key, ...)
```

```
trms(.keys, ...)
```

Arguments

<code>.key</code>	(character(1)) Key passed to the respective dictionary to retrieve the object.
<code>...</code>	(named list()) Named arguments passed to the constructor, to be set as parameters in the paradox::ParamSet , or to be set as public field. See mlr3misc::dictionary_sugar_get() for more details.
<code>.keys</code>	(character()) Keys passed to the respective dictionary to retrieve multiple objects.

Value

- [Terminator](#) for `trm()`.
- list of [Terminator](#) for `trms()`.

Examples

```
trm("evals", n_evals = 10)
```

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