

# Package ‘TRMF’

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**Type** Package

**Title** Temporally Regularized Matrix Factorization

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**Description** Functions to estimate temporally regularized matrix factorizations (TRMF) for forecasting and imputing values in short but high-dimensional time series. Uses regularized alternating least squares to compute the factorization, allows for several types of constraints on matrix factors and natively handles weighted and missing data.

**License** GPL-3

**Encoding** UTF-8

**Imports** Matrix,limSolve,generics

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**VignetteBuilder** knitr

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coef . TRMF	<i>Extract TRMF Coefficients (Fm)</i>
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## Description

Returns the  $F_m$  (transposed) matrix from the matrix factorization  $X_m * F_m$ .

## Usage

```
## S3 method for class 'TRMF'
coef(object, ...)
```

## Arguments

object	a trained TRMF object.
...	other arguments.

## Value

the coefficient matrix,  $t(F_m)$

## Author(s)

Chad Hammerquist

## See Also

[create\\_TRMF](#), [TRMF\\_columns](#), [TRMF\\_trend](#)

## Examples

```
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(runif(40), 4, 10)
Am = xm%%fm+rnorm(210, 0, .2)

# create model
obj = create_TRMF(Am)
out = train(obj)
coef(out)
```

---

components.TRMF	<i>Access TRMF factors</i>
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---

## Description

This function returns the factors (Xm, Fm) from a trained TRMF object

## Usage

```
## S3 method for class 'TRMF'
components(object, XorF = c("Xm", "Fm"), ...)
```

## Arguments

object	trained TRMF object
XorF	which factor to return
...	ignored

## Details

Returns the matrix factors. Could also use `object$Factors$Xm`, `object$Factors$Fm`. If matrix normalization was used in `create_TRMF`, `Xm%%Fm` could look much different than the input data matrix.

## Value

A matrix.

## Author(s)

Chad Hammerquist

## See Also

[create\\_TRMF](#), [TRMF\\_columns](#), [TRMF\\_trend](#)

**Examples**

```
# create test data
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(rnorm(40), 4, 10)
Am = xm%%fm+rnorm(210, 0, .2)

# create model
obj = create_TRMF(Am)
out = train(obj)
plot(out)
components(out, "Xm")
```

---

create_TRMF	<i>Create a TRMF object</i>
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---

**Description**

Creates a TRMF object from a data matrix. This function is always needed to initialize a TRMF model.

**Usage**

```
create_TRMF(dataM, weight = 1,
            normalize = c("none", "standard", "robust", "range"),
            normalize.type = c("global", "columnwise", "rowwise"),
            na.action = c("impute", "fail"))
```

**Arguments**

dataM	The data matrix, each column represents a time series.
weight	An optional matrix of weights to be used in the fitting process. If used, $\sum(w^2 * e^2)$ is minimized.
normalize	Type of scaling/centering for the data. Recommended to reduce bias when using regularization. none does nothing, standard centers with mean, and scales by <code>sd()</code> , robust centers with the median and scales by <code>mad(, constant=1)</code> , range maps to $[-1, 1]$ interval
normalize.type	how should normalization be applied. global scales and centers matrix by one value. columnwise and rowwise normalize each column or row separately.
na.action	what action to take when data contains NAs

**Details**

This function doesn't do any computation, it is the entry point for creating a TRMF model. To train the model or add additional details, see examples. Normalization is recommended in general. Regularization biases the factorization toward zero a little bit, centering changes that to bias towards

the mean. Scaling makes the choosing of regularization parameters easier. If the factorization is to be used for forward forecasting, rowwise normalization is not recommended as it could remove some temporal information.

### Value

create\_TRMF returns an object of `class` "TRMF" to be passed to other TRMF functions.

### Author(s)

Chad Hammerquist

### References

Yu, Hsiang-Fu, Nikhil Rao, and Inderjit S. Dhillon. "High-dimensional time series prediction with missing values." arXiv preprint arXiv:1509.08333 (2015).

### See Also

[train.TRMF](#), [TRMF\\_columns](#), [TRMF\\_trend](#)

### Examples

```
# create test data
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(runif(40), 4, 10)
Am = xm%*%fm+rnorm(210, 0, .2)

# create model
obj = create_TRMF(Am)
obj = TRMF_columns(obj, reg_type = "interval")
obj = TRMF_trend(obj, numTS=4, order=2)
out = train(obj)
plot(out)
```

---

fitted.TRMF

*Extract TRMF fitted values.*

---

### Description

A function to extract fitted values from a trained TRMF object.

### Usage

```
## S3 method for class 'TRMF'
fitted(object, impute = FALSE, ...)
```

**Arguments**

object            a trained TRMF object.  
impute            logical, should imputed values be returned?  
...                other arguments.

**Value**

Fitted values extracted from object. If `impute` is TRUE then entire fitted (unscaled and uncentered) matrix is returned, otherwise there are NAs in the same locations as the time series matrix.

**Author(s)**

Chad Hammerquist

**See Also**

[create\\_TRMF](#), [TRMF\\_columns](#), [TRMF\\_trend](#)

**Examples**

```
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(runif(40), 4, 10)
Am = xm%%fm+rnorm(210, 0, .2)

# create model
obj = create_TRMF(Am)
out = train(obj)
fitted(out)
```

---

impute\_TRMF

*Impute missing values in a matrix*

---

**Description**

Impute missing values in matrix from a pre-trained TRMF object.

**Usage**

```
impute_TRMF(obj)
```

**Arguments**

obj                a trained TRMF object

**Details**

Essentially an accessor function. Replaces the missing values in data matrix with values from the fitted TRMF object.

**Value**

data matrix with missing values imputed

**Author(s)**

Chad Hammerquist

**References**

Yu, Hsiang-Fu, Nikhil Rao, and Inderjit S. Dhillon. "High-dimensional time series prediction with missing values." arXiv preprint arXiv:1509.08333 (2015).

**See Also**

[train.TRMF](#), [create\\_TRMF](#), [TRMF\\_trend](#)

**Examples**

```
# create test data
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(rnorm(40), 4, 10)
Am = xm%%fm+rnorm(210, 0, .2)
Am[sample.int(210, 20)] = NA

# create model
obj = create_TRMF(Am)
obj = TRMF_trend(obj, numTS=4, order=2)
out = train(obj)
impute_TRMF(out)
```

---

NormalizeMatrix

*Matrix Scaling*

---

**Description**

A function for normalizing (scaling and centering) a matrix.

**Usage**

```
NormalizeMatrix(X, method = c("standard", "robust", "range", "none"),
               type = c("global", "rowwise", "columnwise"), na.rm = TRUE)
```

**Arguments**

x	a numeric matrix(like object)
method	type of scaling to perform, standard centers with mean, and scales by sd(), robust centers with the median and scales by mad(, constant=1), range maps to [0-1] interval
type	how should normalization be applied. global scales and centers matrix by one value. columnwise and rowwise normalize each column or row separately.
na.rm	logical value, ignore NA values or not.

**Details**

Scaling and centering quantities are stored as attributes.

**Value**

The possibly centered and scaled matrix. Scaling and centering quantities are stored as attributes.

**Author(s)**

Chad Hammerquist

**Examples**

```
x = matrix(1:10, ncol = 2)
NormalizeMatrix(x)
```

---

plot.TRMF

*Plot Latent Time Series for a TRMF Object*

---

**Description**

Plots all the time series in Xm from a trained TRMF object.

**Usage**

```
## S3 method for class 'TRMF'
plot(x, ...)
```

**Arguments**

x	a trained TRMF object.
...	ignored.

**Value**

No return value, called for side effects



**Author(s)**

Chad Hammerquist

**See Also**[create\\_TRMF](#), [TRMF\\_columns](#), [TRMF\\_trend](#)**Examples**

```

xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(runif(40), 4, 10)
Am = xm%%fm+rnorm(210, 0, .2)

# create model
obj = create_TRMF(Am)
out = train(obj)
plot(out)

```

predict.TRMF

*Predict method for TRMF model fit***Description**

Predict values based on the TRMF fit

**Usage**

```

## S3 method for class 'TRMF'
predict(object, newdata=NULL, ...)

```

**Arguments**

object	A trained TRMF object
newdata	A list with slot $X_m$ and possibly with slots $cX_{reg}$ and $gX_{reg}$
...	other arguments, ignored.

**Details**

If `newdata` is `NULL`, returns fitted model. If `newdata` doesn't have the term  $X_m$  or if it has a different number of columns than the number of latent time series, it will throw an error. If the object also contains a global regression,  $gX_{reg}$  must be present and appropriately sized. If the object also contains a column-wise regression,  $cX_{reg}$  must be present and appropriately sized.

**Value**

Returns a matrix of predictions.

**Author(s)**

Chad Hammerquist

**See Also**[create\\_TRMF](#), [TRMF\\_columns](#), [TRMF\\_trend](#), [train.TRMF](#)**Examples**

```
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(runif(40), 4, 10)
Am = xm%%fm+rnorm(210, 0, .2)

# create model
obj = create_TRMF(Am)
out = train(obj)
fitted(out)
newXm = 1:5
predict(out, newdata=list(Xm=newXm))
```

---

`residuals.TRMF`*Extract TRMF residuals*

---

**Description**

A function to extract residuals from a trained TRMF object.

**Usage**

```
## S3 method for class 'TRMF'
residuals(object, ...)
```

**Arguments**

<code>object</code>	a trained TRMF object.
<code>...</code>	ignored

**Value**

residuals extracted from TRMF object

**Author(s)**

Chad Hammerquist

**See Also**[create\\_TRMF](#), [TRMF\\_columns](#), [TRMF\\_trend](#)

**Examples**

```
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(runif(40), 4, 10)
Am = xm%%fm+rnorm(210, 0, .2)

# create model
obj = create_TRMF(Am)
out = train(obj)
resid(out)
```

---

summary.TRMF

*Summarize TRMF*

---

**Description**

summary method for class "TRMF"

**Usage**

```
## S3 method for class 'TRMF'
summary(object, ...)
```

**Arguments**

object	TRMF object.
...	other arguments.

**Value**

NULL

**Author(s)**

Chad Hammerquist

**See Also**

[create\\_TRMF](#), [TRMF\\_columns](#), [TRMF\\_trend](#)

**Examples**

```
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(runif(40), 4, 10)
Am = xm%%fm+rnorm(210, 0, .2)

# create model
obj = create_TRMF(Am)
out = train(obj)
summary(obj)
summary(out)
```

---

`train.TRMF`*Train a TRMF model*

---

### Description

This function is the "engine" of the TRMF package. It takes a previously created TRMF object and fits it to the data using an alternating least squares algorithm.

### Usage

```
## S3 method for class 'TRMF'  
train(x, numit = 10, ...)
```

### Arguments

<code>x</code>	A TRMF object to be fit.
<code>numit</code>	Number of alternating least squares iterations
<code>...</code>	ignored

### Details

If a coefficient model is not present in object, it adds a L2 regularization model. If no time series models have been added to object, it adds a simple model using [TRMF\\_simple](#).

### Value

`train` returns a fitted object of class "TRMF" that contains the data, all added models, matrix factorization and fitted model. The matrix factors  $X_m$ ,  $F_m$  are stored in `object$Factors$Xm` and `object$Factors$Fm` respectively. Use [fitted](#) to get fitted model, use [resid](#) to get residuals, use [coef](#) to get coefficients ( $F_m$  matrix) and [components](#) to get  $X_m$  or  $F_m$ .

### Author(s)

Chad Hammerquist

### References

Yu, Hsiang-Fu, Nikhil Rao, and Inderjit S. Dhillon. "High-dimensional time series prediction with missing values." arXiv preprint arXiv:1509.08333 (2015).

### See Also

[create\\_TRMF](#), [TRMF\\_columns](#), [TRMF\\_trend](#)

**Examples**

```
# create test data
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(rnorm(40), 4, 10)
Am = xm%%fm+rnorm(210, 0, .2)

# create model
obj = create_TRMF(Am)
out = train(obj)
plot(out)
```

TRMF\_ar

*Add an Auto-Regressive Regularization Model to a TRMF Object.***Description**

Creates a regularization scheme that constrains latent time-series based on auto-regressive parameters and adds it to a TRMF object. In matrix optimization form, it adds the following term to the TRMF cost function:  $R(x) = \lambda D^2 \|w(DX_s)\|^2 + \lambda A^2 \|X_s\|^2$  where  $X_s$  is sub-set of the  $X_m$  matrix controlled by this model and  $D$  is a matrix that corresponds to an auto-regressive model.

**Usage**

```
TRMF_ar(obj, numTS = 1, AR, lambdaD=1, lambdaA=0.0001, weight=1)
```

**Arguments**

obj	A TRMF object
numTS	number of latent time series in this model
lambdaD	regularization parameter for temporal constraint matrix
lambdaA	regularization parameter to apply simple L2 regularization to this time series model
weight	optional vector of weights to weight constraints, i.e. $R(x) = \lambda D^2 \ w(D\%*X)\ ^2$
AR	vector of autoregressive parameters. No checks are performed

**Details**

Setting  $AR = c(1)$  gives a random walk model, same as `TRMF_trend(..., order=1)`

**Value**

Returns an updated object of class TRMF.

**Author(s)**

Chad Hammerquist

**References**

Yu, Hsiang-Fu, Nikhil Rao, and Inderjit S. Dhillon. "High-dimensional time series prediction with missing values." arXiv preprint arXiv:1509.08333 (2015).

**See Also**

[create\\_TRMF](#), [TRMF\\_columns](#), [TRMF\\_trend](#)

**Examples**

```
# create test data
xm = matrix(rnorm(80),20,4)
fm = matrix(rnorm(40),4,10)+1
Am = xm%%fm+rnorm(200,0,.1)

# create model
obj = create_TRMF(Am)
obj = TRMF_columns(obj,reg_type = "interval")
obj = TRMF_ar(obj,numTS=2,AR=c(0.5),lambdaD=4)
out = train(obj)
plot(out)
```

---

TRMF\_columns

*Add regularization model to TRMF object*

---

**Description**

Adds a regularization model to TRMF object created by `create_TRMF()` to constrain the fitting process of the coefficient matrix.

TRMF\_coefficient is a (soon to be deprecated) alias for TRMF\_columns.

**Usage**

```
TRMF_columns(obj,
  reg_type = c("l2", "nnls", "constrain", "interval", "none"), lambda = 0.0001)
TRMF_coefficients(obj,
  reg_type = c("l2", "nnls", "constrain", "interval", "none"), lambda = 0.0001)
```

**Arguments**

obj	TRMF object created by <code>create_TRMF()</code>
reg_type	regularization type to apply when fitting TRMF model. <code>l2</code> regularizes by simple sum of squares, <code>nnls</code> forces coefficients to be non-negative. <code>constrain</code> constrains coefficients to be non-negative and to sum to 1. <code>interval</code> constrains coefficients to the interval [0-1]
lambda	L2 regularization parameter used for all regularization types. If NULL, uses lambda set in <code>create_TRMF()</code> .

**Details**

This function doesn't do any computations, it just sets up regularization parameters for the coefficient matrix. This function should only be called once on a TRMF object. If called twice, it will overwrite previous model with a warning.

**Value**

Returns an updated object of class TRMF.

**Author(s)**

Chad Hammerquist

**References**

Yu, Hsiang-Fu, Nikhil Rao, and Inderjit S. Dhillon. "High-dimensional time series prediction with missing values." arXiv preprint arXiv:1509.08333 (2015).

**See Also**

[train.TRMF](#), [create\\_TRMF](#), [TRMF\\_trend](#)

**Examples**

```
# create test data
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(abs(rnorm(40)), 4, 10)
Am = xm%%fm+rnorm(210, 0, .2)

# create model
obj = create_TRMF(Am)
obj = TRMF_columns(obj, reg_type = "nnls")
out = train(obj)
plot(out)
```

TRMF\_es

*Add exponential smoothing regularization model to a TRMF object.***Description**

Creates a regularization scheme that favors exponentially smoothed solutions and adds it to a TRMF object. In matrix optimization form, it adds the following term to the TRMF cost function:  $R(x) = \lambda D^2 \|w(DX_s)\|^2 + \lambda A^2 \|X_s\|^2$  where  $X_s$  is sub-set of the  $X_m$  matrix controlled by this model and  $D$  is a matrix with weights from exponential smoothing.

**Usage**

```
TRMF_es(obj,numTS = 1,alpha=1,es_type=c("single","double"),
        lambdaD=1,lambdaA=0.0001,weight=1)
```

**Arguments**

obj	A TRMF object
numTS	number of latent time series in this model
lambdaD	regularization parameter for temporal constraint matrix
lambdaA	regularization parameter to apply simple L2 regularization to this time series model
weight	optional vector of weights to weight constraint, i.e. $R(x) = \lambda D^2 \ w(D\%*\%X)\ ^2$
es_type	type of exponential smoothing. "double" does Brown's double exponential smoothing.
alpha	exponential smoothing parameter, constrained to be in the interval [0,1]

**Details**

This creates a non-sparse constraint matrix which could slow training down for longer time series.

**Value**

Returns an updated object of class TRMF.

**Author(s)**

Chad Hammerquist

**References**

Yu, Hsiang-Fu, Nikhil Rao, and Inderjit S. Dhillon. "High-dimensional time series prediction with missing values." arXiv preprint arXiv:1509.08333 (2015).

[https://en.wikipedia.org/wiki/Exponential\\_smoothing](https://en.wikipedia.org/wiki/Exponential_smoothing)



**See Also**

[create\\_TRMF](#), [TRMF\\_columns](#), [TRMF\\_trend](#), [TRMF\\_seasonal](#)

**Examples**

```
# create test data
xm = cbind(cumsum(rnorm(20)),cumsum(rnorm(20)))
fm = matrix(runif(20),2,10)
Am = xm%%fm+rnorm(200,0,.2)

# create model
obj = create_TRMF(Am)
obj = TRMF_es(obj,numTS=2,alpha=0.5)
out = train(obj)
plot(out)
```

---

TRMF_regression	<i>Add external regressors to TRMF object</i>
-----------------	---

---

**Description**

A function to add external regressors to a TRMF object.

**Usage**

```
TRMF_regression(obj, Xreg, type = c("global", "columnwise"))
```

**Arguments**

obj	TRMF object created by <code>create_TRMF()</code>
Xreg	Vector or matrix of external regressors. If <code>type = "columnwise"</code> , Xreg can be a matrix or array, but the first two dimensions must match those of the data matrix.
type	how are the regressors added to the model. If <code>type = "global"</code> the matrix factorization includes all the regressors. If <code>type = "columnwise"</code> each column in the data matrix is regressed of the corresponding column of Xreg.

**Details**

The coefficients model for the regressors are subject to the same regularization as the rest of the matrix factorization. Only one columnwise and one global model should be used in the same model. Both types can be include in the same model though.

**Value**

Returns an updated object of class TRMF.

**Author(s)**

Chad Hammerquist

**See Also**[create\\_TRMF](#), [TRMF\\_columns](#), [TRMF\\_trend](#)**Examples**

```

# ~ Global regression example ~
# create test data
bb = (-10:10)/10
xReg = 10*cos(bb*10)
xm = poly(x = bb,degree=3)
fm = matrix(rnorm(40),4,10)
Am = cbind(xReg,xm)%*%fm+rnorm(210,0,.2)

# creat model and fit
obj = create_TRMF(Am)
obj = TRMF_trend(obj,numTS=3,order=2)
obj = TRMF_regression(obj,Xreg=xReg,type="global")
out = train(obj)
plot(out)

# ~ columnwise regression example ~
# create test data
bb = (-10:10)/10
xm = poly(x = bb,degree=4)
fm = matrix(rnorm(84),4,21)
Am = xm%*%fm+rnorm(441,0,.2)

layers = array(0,dim=c(21,21,2))
layers[, ,1] = 2*cos(2*bb)%o%sin(4*bb)
layers[, ,2] = 2*sqrt(abs(bb%o%bb))
nAm = Am+layers[, ,1]+layers[, ,2]

# creat model and fit
obj = create_TRMF(nAm)
obj = TRMF_trend(obj,numTS=4,order=2)
obj = TRMF_regression(obj,Xreg=layers,type="columnwise")
out = train(obj)
plot(out)

```

**Description**

Creates a regularization scheme that favors seasonally varying solutions and adds it to a TRMF object. In matrix optimization form, it adds the following term to the TRMF cost function:  $R(x) = \lambda D^2 \|w(DX_s)\|^2 + \lambda A^2 \|X_s\|^2$  where  $X_s$  is sub-set of the  $X_m$  matrix controlled by this model and  $D$  is a (with a lag of  $\text{freq}$ ) finite difference matrix.

**Usage**

```
TRMF_seasonal(obj,numTS = 1,freq = 12,sumFirst=FALSE,lambdaD=1,lambdaA=0.0001,weight=1)
```

**Arguments**

obj	A TRMF object
numTS	number of latent time series in this model
lambdaD	regularization parameter for temporal constraint matrix
lambdaA	regularization parameter to apply simple L2 regularization to this time series model
weight	optional vector of weights to weight constraints, i.e. $R(x) = \lambda D^2 \ w(D\%*X)\ ^2$
freq	The frequency of the seasonal time series model. Minimize the differences of lag = freq
sumFirst	minimize the sum of first freq elements in time series

**Details**

TRMF\_seasonal(freq=N) fits a lag N random walk. For monthly data, use freq=12, for quarterly data, freq=4. If sumFirst = TRUE, the sum of the first freq elements in the latent time series are also minimized. This can be used to help force the seasonal component to vary around a zero mean.

**Value**

Returns an updated object of class TRMF.

**Author(s)**

Chad Hammerquist

**References**

Yu, Hsiang-Fu, Nikhil Rao, and Inderjit S. Dhillon. "High-dimensional time series prediction with missing values." arXiv preprint arXiv:1509.08333 (2015).

**See Also**

[create\\_TRMF](#), [TRMF\\_columns](#), [TRMF\\_simple](#), [TRMF\\_trend](#)

**Examples**

```
# create test data
tm = 3*poly(x = (-20:20)/10,degree=3)
sm = diffinv(rnorm(29,0,.1),lag=12,xi=(-5:6)/6)
xm = cbind(sm,tm)
fm = matrix(runif(40),4,10)
Am = xm%%fm+rnorm(410,0,.1)

# create model
obj = create_TRMF(Am)
obj = TRMF_columns(obj,reg_type = "interval")
obj = TRMF_trend(obj,numTS=3,order=2)
obj = TRMF_seasonal(obj,numTS=1,freq=12,lambdaD=5)
out = train(obj)
plot(out)
```

---

TRMF\_simple

Add L2 regularization model to a TRMF object

---

**Description**

Creates an L2 regularization and adds it to a TRMF object. In matrix optimization form, it adds the following term to the TRMF cost function:  $R(x) = \lambda A^2 \|w(X_s)\|^2$  where  $X_s$  is sub-set of the  $X_m$  matrix controlled by this model.

**Usage**

```
TRMF_simple(obj,numTS = 1,lambdaA=0.0001,weight=1)
```

**Arguments**

obj	A TRMF object
numTS	number of latent time series in this model
lambdaA	regularization parameter to apply simple L2 regularization to this time series model
weight	optional vector of weights to weight constraints, i.e. $R(x) = \lambda A^2 \ w * X\ ^2$

**Details**

This is called by `train_TRMF` if the TRMF object doesn't have any time series models.

**Value**

Returns an updated object of class TRMF.

**Author(s)**

Chad Hammerquist

**References**

Yu, Hsiang-Fu, Nikhil Rao, and Inderjit S. Dhillon. "High-dimensional time series prediction with missing values." arXiv preprint arXiv:1509.08333 (2015).

**See Also**

[create\\_TRMF](#), [TRMF\\_columns](#), [TRMF\\_seasonal](#), [TRMF\\_trend](#)

**Examples**

```
# create test data
xm = matrix(rnorm(160),40,4)
fm = matrix(runif(40),4,10)
Am = xm%%fm+rnorm(400,0,.1)

# create model
obj = create_TRMF(Am)
obj = TRMF_simple(obj,numTS=4,lambdaA=0.1)
out = train(obj)
plot(out)
```

TRMF\_trend

*Add Trend Model to a TRMF Object***Description**

Creates a regularization scheme that favors trend-like solutions and adds it to a TRMF object. In matrix optimization form, it adds the following term to the TRMF cost function:  $R(x) = \lambda D^2 \|w(DX_s)\|^2 + \lambda A^2 \|X_s\|^2$  where  $X_s$  is sub-set of the  $X_m$  matrix controlled by this model and  $D$  is a finite difference matrix.

**Usage**

```
TRMF_trend(obj,numTS = 1,order = 1,lambdaD=1,lambdaA=0.0001,weight=1)
```

**Arguments**

obj	A TRMF object
numTS	number of latent time series in this model
order	The order of derivative for finite difference constraint matrix. Fractionally and negative values allowed.
lambdaD	regularization parameter for temporal constraint matrix
lambdaA	regularization parameter to apply simple L2 regularization to this time series model
weight	optional vector of weights to weight constraints, i.e. $R(x) = \lambda D^2 * \ w*(D\%*X)\ ^2$

## Details

An arbitrary number of time series models can be added. `TRMF_trend(order = 1)` fits a random walk. `TRMF_trend(order = 2)` fits a cubic smoothing spline. For a single time series, `TRMF_trend(order = 2)` is basically equivalent to the Hodge-Prescot filter. A fractional value for `order` minimizes a squared fractional derivative. A negative value minimizes a (possibly fractional order) squared integral of time-series. Using a fractional or negative order for `TRMF_trend` or using `TRMF_es` could drastically reduce the sparsity of constraint matrix and slow down training. Fractional or negative order has only been lightly tested, so use with care.

## Value

Returns an updated object of class `TRMF`.

## Author(s)

Chad Hammerquist

## References

Yu, Hsiang-Fu, Nikhil Rao, and Inderjit S. Dhillon. "High-dimensional time series prediction with missing values." arXiv preprint arXiv:1509.08333 (2015).

## See Also

[create\\_TRMF](#), [TRMF\\_columns](#), [TRMF\\_simple](#), [TRMF\\_seasonal](#)

## Examples

```
# create test data
xm = poly(x = (-10:10)/10, degree=4)
fm = matrix(runif(40), 4, 10)
Am = xm*%fm+rnorm(210, 0, .1)

# create model
obj = create_TRMF(Am)
obj = TRMF_columns(obj, reg_type = "interval")
obj = TRMF_trend(obj, numTS=4, order=2, lambdaD=2)
out = train(obj)
plot(out)

# more complex model
require(magrittr) # for pipes

obj = create_TRMF(Am)%>%
  TRMF_columns(reg_type = "interval")%>%
  TRMF_trend(numTS=2, order=1, lambdaD=4)%>%
  TRMF_trend(numTS=2, order=2, lambdaD=4)%>%
  TRMF_trend(numTS=1, order=1.5)

out = train(obj)
```

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plot(out)

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